# THE ANNALS

# of

# **PROBABILITY**

AN OFFICIAL JOURNAL OF
THE INSTITUTE OF MATHEMATICAL STATISTICS

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