

$$\begin{aligned}
 (25) \quad S_n(z; f) &= S_n(z; g) + \sum_{k=1}^N S_n(z; g_k y_{m_k}) \\
 &= \frac{1}{2\pi i} \int_{\Gamma_R} \frac{W_{n+1}(t) - W_{n+1}(z)}{W_{n+1}(t)} \frac{g(t)}{t-z} dt \\
 &\quad + \sum_{k=1}^N Y_{m_k} \left( \frac{W_{n+1}(t) - W_{n+1}(z)}{W_{n+1}(t)} \frac{g_k(t)}{t-z}; a_k \right).
 \end{aligned}$$

By the method similar to the proof of Theorem 3, we have

$$\begin{aligned}
 n^{m_k} \left( \frac{\phi(a_k)}{w} \right)^{n+1} S_n(z; g_k y_{m_k}) &= n^{m_k} \left( \frac{\phi(a_k)}{w} \right)^{n+1} Y_{m_k} \left( \frac{W_{n+1}(t) - W_{n+1}(z)}{W_{n+1}(t)} \frac{g_k(t)}{t-z}; a_k \right) \\
 &\sim n^{m_k} \phi^{n+1}(a_k) \frac{W_{n+1}(z)}{w^{n+1}} Y_{m_k} \left( \frac{1}{W_{n+1}(t)} \frac{g_k(t)}{t-z}; a_k \right) \\
 &\sim n^{m_k} \phi^{n+1}(a_k) \lambda(\phi(z)) Y_{m_k} \left( w^{-(n+1)} \frac{g_k(t)}{\lambda(\phi(t))(t-z)}; a_k \right) \\
 &\quad + n^{m_k} \phi^{n+1}(a_k) \lambda(\phi(z)) Y_{m_k} \left[ w^{-(n+1)} \left( \frac{1}{\lambda(w)} - \frac{t^{n+1}}{W_{n+1}(t)} \right) \frac{g_k(t)}{t-z}; a_k \right] \\
 &\sim (-1)^{m_k} [\phi(a_k)]^{m_k} \lambda(\phi(z)) \frac{g_k(a_k)}{\lambda(\phi(a_k))(a_k-z)} = B_k \neq 0,
 \end{aligned}$$

for  $z$  exterior to  $\Gamma_R$ .

As a generalization of Theorem 4, a theorem follows by Lemma 3. That is,

**Theorem 5.** *Let  $D$  be a closed limited points set with the capacity  $\Delta$  whose complement  $K$  with respect to the extended plane is connected and regular in the sense that  $K$  possesses a Green's function with pole at infinity. Let  $w = \phi(z)$  map  $K$  onto the region  $|w| > 1$  so that the points at infinity correspond to each other. Let  $W_n(z)$  be the polynomials of respective degrees,  $n$  which satisfy the condition (24) and  $f(z)$  be a function such that represented by (23).*

*Then the sequence of polynomials  $S_n(z; f)$  of respective degrees  $n$  found by interpolation to  $f(z)$  in all the zeros of  $W_{n+1}(z)$  diverges at every point exterior to  $\Gamma_R$ . Moreover, we have*

$$(26) \quad \lim_{n \rightarrow \infty} \left| n^p \left( \frac{R}{\phi(z)} \right)^n S_n(z; f) \right| > 0; \quad |\phi(z)| > R > 1,$$

where  $p$  is the minimum of real parts of  $m_k$  in (23).

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 Additions and Corrections to Tetsujiro Kakehashi:

“The Divergence of Interpolations. I”

(Proc. Japan Acad., 30, No. 8, 741-745 (1954))

Page 742, equation (5), for “ $\frac{1}{2\pi i}$ ” read “ $\frac{(-1)^m}{2\pi i}$ ”.

Page 744, line 4, for “ $\lim_{n \rightarrow \infty} \frac{1 \cdot 2 \cdots (n-1)}{z(z+1) \cdots (z+n-1)}$ ”  
 read “ $\lim_{n \rightarrow \infty} \frac{1 \cdot 2 \cdots (n-1)}{z(z+1) \cdots (z+n-1)} n^z$ ”