THE ANNALS of PROBABILITY

AN OFFICIAL JOURNAL OF
THE INSTITUTE OF MATHEMATICAL STATISTICS

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$$(2\pi)^{-1} \ {
m or} \ 1/(2\pi) \ {
m to} \ {1\over 2\pi}.$$
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