Letter to the Editor

Comment on "A New Second-Order Iteration Method for Solving Nonlinear Equations"

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Kang et al. claimed that they obtained a new iteration formulation for nonlinear algebraic equations; however the "new" formulation was first derived in 2007 by the variational iteration method.

Recently Kang et al. studied the following algebraic equation:

$$x = g\left(x\right) \tag{1}$$

and obtained the following iteration formulation [1, Equation (13)]:

$$x_{n+1} = \frac{-x_n g'(x_n) + g(x_n)}{1 - g'(x_n)}, \quad g'(x_n) \neq 1.$$
(2)

Kang et al. claimed that this was a new iteration formulation [1]; however, a more general iteration formulation has appeared in 2007 [2].

Consider a nonlinear algebraic equation

$$f(x) = 0. \tag{3}$$

By the variational iteration method [2], the following iteration formulation was obtained [2, Equation (7)]:

$$\begin{aligned} x_{n+1} &= x_n - \frac{h(x_n) f(x_n)}{h(x_n) f'(x_n) + h'(x_n) f(x_n)}, \\ &\quad h(x_n) f'(x_n) + h'(x_n) f(x_n) \neq 0, \end{aligned}$$
(4)

where h(x) is an auxiliary function.

Choosing h(x) = 1 and f(x) = x - g(x) in (4), we have

$$x_{n+1} = x_n - \frac{x_n - g(x_n)}{1 - g'(x_n)} = \frac{-x_n g'(x_n) + g(x_n)}{1 - g'(x_n)}.$$
 (5)

This is exactly (2).

Using the basic idea of the variational iteration method as illustrated in [2] (see (1)-(8) in [2]), we can construct an iteration formulation for (1) in the form

$$x_{n+1} = g(x_n) + \lambda \left(g(x_n) - x_n\right),\tag{6}$$

where λ is a Lagrange multiplier. To identify the multiplier, we set (see [2, Equation (4)])

$$\frac{dx_{n+1}}{dx_n} = g'\left(x_n\right) + \lambda\left(g'\left(x_n\right) - 1\right) = 0,\tag{7}$$

from which the multiplier can be identified, which is

$$\lambda = -\frac{g'(x_n)}{g'(x_n) - 1}.$$
(8)

This results in

$$\begin{aligned} x_{n+1} &= g\left(x_{n}\right) - \frac{g'\left(x_{n}\right)}{g'\left(x_{n}\right) - 1} \left(g\left(x_{n}\right) - x_{n}\right) \\ &= \frac{-g\left(x_{n}\right) + x_{n}g'\left(x_{n}\right)}{g'\left(x_{n}\right) - 1}. \end{aligned}$$
(9)

Remark 1. Equation (9) is exactly (2) or (4) when h(x) = 1 and f(x) = x - g(x).

Remark 2. Equation (7) is exactly equivalent to $g'_{\theta}(x) = 0$ in [1].

Remark 3. θ in [1] is exactly equivalent to the Lagrange multiplier in (7).

Remark 4. The derivation process is the same as that given in [2].

It can be concluded that the so-called new iteration method is a special case of He 2007 formulation; various modifications of Newton iteration formulations are available in [2–7].

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