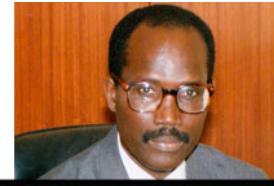


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***Hamet Seydi, Gane Samb Lo & Aboubakary
Diakhaby, Editors.***

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