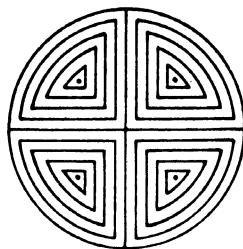


# The Rocky Mountain Journal of Mathematics

Volume 10, 1980



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Printed by The Texas Tech Press  
Texas Tech University  
Lubbock, Texas, U.S.A.

## **INTRODUCTION TO THIS ISSUE**

**PAWEL SZEPTYCKI**

This volume is dedicated to Nachman Aronszajn on the occasion of his 70th birthday.

Some of the papers in this volume were presented at the Conference on Functional Analysis and Related Topics held at the University of Kansas on May 17, 18, 19, 1977. The organizers of the Conference gratefully acknowledge the financial help of the University of Kansas and of the National Science Foundation, without which much of the work and the Conference would not have been possible.



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