# THE ANNALS of STATISTICS

# AN OFFICIAL JOURNAL OF THE INSTITUTE OF MATHEMATICAL STATISTICS

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Vol. 2, No. 1—January 1974

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The Annals of Statistics, Volume 2, Number 1, January 1974. Published bimonthly in January, March, May, July, September, and November by The Institute of Mathematical Statistics, MR IV—Room 131, University of California, S.F., San Francisco, California 94122.

Mail to the Annals of Statistics should be addressed to either the Editor, Managing Editor or the Treasurer as described above. It should not be addressed to Waverly Press.

### PRINTED AT THE

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The classification numbers representing the primary and secondary subjects of the article may be found with instructions for its use, as an Appendix to Mathematical Reviews Index to Volume 39, June 1970. (See, also, The Notices of the American Mathematical Society, June 1970, pp. 616-618, for more details.) The key words and phrases should describe the subject matter of the article; generally they should be taken from the body of the paper.

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$$(a+b)/(c+d)$$
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