# THE ANNALS of PROBABILITY

AN OFFICIAL JOURNAL OF
THE INSTITUTE OF MATHEMATICAL STATISTICS

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American Mathematical Society 1970 subject classifications. Primary—; Secondary—. Key words and phrases.

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