# THE ANNALS ISSN (0090-5364) of **STATISTICS**

# AN OFFICIAL JOURNAL OF THE INSTITUTE OF MATHEMATICAL STATISTICS

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