

Minimal Models and Extremal Rays (Kyoto, 2011)

**ADVANCED STUDIES  
IN PURE MATHEMATICS 70**

Chief Editor of the Series: Yoshihiro Tonegawa (Tokyo Institute of Technology)

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**Minimal Models and Extremal Rays  
(Kyoto, 2011)**

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*Edited by the Mathematical Society of Japan.*

*Published by the Mathematical Society of Japan.*

*Distributed by the Mathematical Society of Japan, the American Mathematical Society and the World Scientific Publishing Co., Ltd.*

*Distributed exclusively in North America by the American Mathematical Society.*

*Advanced Studies in Pure Mathematics 70*

*ISBN 978-4-86497-036-5*

PRINTED IN JAPAN

by Livretech Co., Ltd.

*2010 Mathematics Subject Classification.*

*Primary 14-06.*

*Secondary 14E30, 14B07, 14D05, 14E07, 14E15, 14F17, 14F18, 14J17, 14J28, 14J32, 14J45, 53D05.*

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