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# **Interface Profile of the Ising Ferromagnet** in Two Dimensions

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**Abstract.** The interface profile of the two-dimensional Ising ferromagnet is obtained for all temperatures in the thermodynamic limit. The width of the interface depends on its length as  $(length)^{1/2}$ .

#### 1. Introduction

Recently considerable effort has been devoted to the unravelling of the phenomenon of phase separation in the Ising ferromagnet or in the equivalent lattice gas [1, 2, 3]. This paper reports on exact calculation of the surface tension and interface profile for the two dimensional case with nearest neighbour interactions and zero "gravitational" field [0]. First we shall review briefly exact results already established and then we shall relate our computation to them.

## 2. Notation and Results

Let  $\Lambda$  be a crystal lattice in d dimensions with unit edges; it may therefore be regarded as a subset of  $\mathbb{Z}^d$ . At each vertex i let there be a spin  $\sigma_i = \pm 1$ . The energy of a spin configuration  $\{\sigma\}$  is given by:

$$E_{\Lambda}\{\sigma\} = -J \sum_{\langle i,j \rangle \subset \Lambda} \sigma_{i} \sigma_{j} - \mathcal{B}_{\Lambda}\{\sigma\}$$
 (2.1)

with associated probability measure

$$p_{\Lambda,\mathscr{B}}(\{\sigma\}) = Z^{-1} \exp{-\beta E_{\Lambda}(\{\sigma\})}. \tag{2.2}$$

The sum in (2.1) is over nearest neighbour pairs on  $\Lambda$  and  $\mathcal{B}_{\Lambda}(\{\sigma\})$  is a boundary term [1], examples of which will be encountered later.

Let  $\sigma_A$  be defined for  $A \subset \mathbb{Z}^d$  by

$$\sigma_A = \prod_{i \in A} \sigma_i \tag{2.3}$$

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