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Attempt of an Axiomatic Foundation of Quantum Mechanics and More General Theories VI*

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Abstract. This contribution continues the series of papers [2, 4, 5, 12] treated by Ludwig and collaborators. It is based on the generalized frame given in [6]; there Ludwig has set up an "infinite" axiomatic scheme as extension of the "finite" system [4, 5]. The results of [12] are then proved for a "locally finite" case; they lead to an extended representation theorem.

I. Introduction

In his paper "Notes on Axioms for Quantum Mechanics" [10] MacLaren has set up the final axiom:

(C) The set of all atoms of every finite sublattice of the orthomodular lattice G of decision effects is compact in the norm topology.

This axiom guarantees that the division ring which is constructed over G is the real, complex or quaternionic numbers [14].

We base here on Ludwig's general axiomatic scheme ([6], III.) restricted by [6], III. § 18 condition V_3 ("locally-finite" case!) which is a generalization of the "finite" system given in [4, 5]. Within this frame the purpose of this paper is

1. to prove a slightly weaker form (\underline{C}) (Lemma 8 in part III), of statement (\underline{C}),

2. to show that $(\underline{\mathbf{C}})$ is sufficient to exclude discontinuous and disconnected division rings,

3. to give further topological properties of the lattice G.

II. Preliminaries

In the following largely is used the punctuation and terminology of [12]. We give a somewhat modified summary of Ludwig's conclusions [6] which are different from those used in [12].

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