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BUCHSBAUM SUBVARIETIES OF CODIMENSION 2 IN \mathbf{P}^n

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Over the past several years there has been considerable activity in the topics of Buchsbaum rings and arithmetically Buchsbaum projective curves, some of which was described in the book [3]. Recall that a local (resp. graded) ring A is Buchsbaum if the difference $l_A(A/\mathfrak{x}A) - e(\mathfrak{x}, A)$ is independent of the (homogeneous) system of parameters \mathfrak{x} , where l_A and e are the length and multiplicity respectively. A subvariety Y in \mathbf{P}^n is called arithmetically Buchsbaum if its homogeneous coordinate ring $\bigoplus H^0(\mathcal{O}_{\mathbf{P}^n}(k))/\bigoplus H^0(I_Y(k))$ is Buchsbaum. This in particular implies

(1) *the multiplication map $H^p(I_Y(k)) \xrightarrow{x} H^p(I_Y(k+1))$ is 0 for all $x \in H^0(\mathcal{O}_{\mathbf{P}^n}(1))$ and $1 \leq p \leq \dim Y$.*

Conversely, if we have (1) and

(2) *whenever $H^p(I_Y(k)) \neq 0 \neq H^q(I_Y(h))$ for $1 \leq p < q \leq \dim Y$, then $(p+k) - (q+h) \neq 1$,*

then Y is arithmetically Buchsbaum (cf. [3]). (Note that (2) is vacuous if $n = 3$.)

The purpose of this note is to announce a structure theorem for arithmetically Buchsbaum subvarieties of codimension 2 satisfying (2). We also give several applications of this theorem, including some inequalities among the number and the degree of the generators of the homogeneous ideal I_Y and the degree of Y , nonexistence of nonsingular codimension 2 Buchsbaum subvarieties satisfying (2), in \mathbf{P}^n for $n \geq 6$, and classification of the nonsingular ones for $n \leq 5$.

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