RESEARCH ANNOUNCEMENTS

ON THE ABUNDANCE OF APERIODIC BEHAVIOUR FOR MAPS ON THE UNIT INTERVAL¹

BY P. COLLET AND J.-P. ECKMANN

Continuous maps from the interval [0, 1] to itself have been studied for some time as simple models of dynamical systems with discrete time. In particular, the map $x \mapsto 1 - 2|x - \frac{1}{2}|$ has no stable periodic orbit on [0, 1]. In the paper [1] we show that such behaviour is very common among the members of a parametrized family of maps which contain a quadratic critical point.

Let $0 < \delta < \frac{1}{2}$ and define the map $f_{\delta} \colon [0, 1] \to [0, 1]$ by

$$f_{\delta}(x) = \begin{cases} 1 - \delta - (x - \frac{1}{2})^2 / \delta & \text{for } x \in [\frac{1}{2} - \delta, \frac{1}{2} + \delta], \\ 1 - 2 |x - \frac{1}{2}| & \text{for } x \in [0, \frac{1}{2} - \delta] \cup [\frac{1}{2} + \delta, 1]. \end{cases}$$

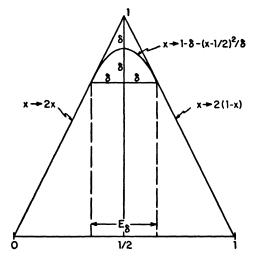


FIGURE 1. The function f_{δ} for $\delta = 0.15$.

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