

tion of linear functions of ordered dyads  $X_{m+1}(\alpha) = \sum x_j \alpha_j \alpha_j$  ( $j = 1, 2, \dots, m+1$ ) with coefficients  $x_j$  in a suitable domain  $D$  (field  $F$ ) relatively to any given abstract group  $G$  of order  $m+1$  ( $m = 1, 2, \dots$ ) represented as a regular group of configurational sets of dyads on  $m+1$  elements. Two dyads  $\alpha_i \alpha_j$  and  $\alpha_k \alpha_l$  are then equivalent if and only if they occur in the same configurational set of dyads. Multiplication is determined by  $\alpha_i \alpha_j \times \alpha_k \alpha_l = \alpha_i \alpha_k$  and by the preceding equivalences. Other instances of dyadic representation of linear algebras are given by two examples: 1.  $X_2(\alpha) = x_1 \alpha_1 \alpha_1 + x_2 \alpha_2 \alpha_2$  with equivalences  $\alpha_1 \alpha_1 = \alpha_2 \alpha_2$ ,  $\alpha_1 \alpha_2 = -\alpha_2 \alpha_1$ . 2.  $X_4(\alpha) = \sum x_j \alpha_j \alpha_j$  ( $j = 1, 2, 3, 4$ ) with equivalences corresponding to those given by the author (*Math. Ann.* vol. 69 p. 584). In both examples multiplication is determined by  $\alpha_i \alpha_j \times \alpha_k \alpha_l = \alpha_i \alpha_k$  and by the associated equivalences. (Received July 11, 1946.)

278. M. C. Sholander: *On the existence of the inverse operation in certain spaces.*

In a set  $S$  of elements  $x, y, \dots$  which admits a binary operation—here denoted by multiplication—an element  $a$  will be called regular if both (i)  $ax = ay$  implies  $x = y$  and (ii)  $xa = ya$  implies  $x = y$ . An element  $a$  will be called proper if for each element  $b$  in  $S$  there exist unique solutions  $x$  and  $y$  in  $S$  for the equations  $ax = b$  and  $ya = b$ . It is well known that if the multiplication is commutative and associative  $S$  can be imbedded in a space  $S'$  of the same type in such a way that all elements regular in  $S$  are proper in  $S'$ . In this paper it is shown the imbedding process can also be carried out in case the multiplication is one satisfying the alternation law  $(ab)(cd) = (ac)(bd)$  and in case the regular elements of  $S$  are closed under multiplication. Thus if all elements of  $S$  are regular,  $S'$  is a quasi-group of a type studied, for example, by D. C. Murdoch (*Trans. Amer. Math. Soc.* vol. 49 (1941) pp. 392–409) and R. H. Bruck (*Trans. Amer. Math. Soc.* vol. 55 (1944) pp. 19–52). Various conditions which insure the necessary closure property in  $S$  are given in the paper. (Received July 26, 1946.)

279. J. M. Thomas: *Eliminants.*

If  $R(a, b)$  denotes the resultant to two polynomials  $x(t), y(t)$  whose constant terms are  $a, b$ , the polynomial  $R(a-x, b-y)$  in the two indeterminates  $x, y$  is the *eliminant*  $E(x, y)$  of  $x(t), y(t)$ . This paper (i) proves  $E(x, y) = f^k$ , where  $f$  is an irreducible polynomial and  $k$  is a positive integer; (ii) proves  $E(x, y)$  is reducible ( $1 < k$ ) if and only if  $x(t), y(t)$  are also polynomials in a second parameter which is itself a polynomial of degree at least two in  $t$ ; (iii) expresses in terms of  $E(x, y)$  algebraic conditions that a single polynomial  $y(t)$  be a polynomial in  $x(t)$  of degree  $k$ , where  $1 < k < \deg y$  (these last polynomials have been called by Ritt composite polynomials, *Trans. Amer. Math. Soc.* vol. 23 (1922) pp. 51–66). (Received July 27, 1946.)

280. J. H. M. Wedderburn: *Note on Goldbach's theorem.*

It is shown in this note that, if  $p$  and  $q$  are primes and  $r = (p+q)/2$  is a prime, then  $p-q$  is a multiple of 12 unless  $r$  has the form  $2p-3$  or, when unity is reckoned as a prime, also  $r = 2p-1$ . The proof is elementary and depends on reducing modulo 12. Similar statements apply if  $q$  is replaced by  $-q$ . (Received July 30, 1946.)

#### ANALYSIS

281. R. P. Agnew: *Methods of summability which evaluate sequences of zeros and ones summable  $C_1$ .*