which the oscillation is not less than a given positive number form a closed set; the Du Bois-Reymond theorems on integration; the Sierpinski theorem; and others. The new concept lends itself readily to broad generalizations, and its simplicity suggests the possibility of advantageous use even in the usual theory.

10. Let  $a_{ik}$  be the general element of the infinite determinant D and assume the convergence of  $\Sigma |a_{ik}|$ . By comparison with an infinite product Professor Brenke obtains the following results, of which (d) is a well-known theorem, from which also (a) might be derived: (a) D converges absolutely to the value 0; (b) if the elements of any number of rows or columns of D are replaced by quantities less in absolute value than a positive constant, the new determinant converges absolutely; (d) von Koch's "normal determinant" converges absolutely; (e) a normal determinant remains absolutely convergent if elements  $a_{ik}$  are replaced as in (c).

11. Professor Davis shows that if the difference between two complex vectors in space is  $\delta_1 + \sqrt{-1}\delta_2$  and if k is  $UV\delta_1\delta_2$ , then the square of the distance between the complex vectors is  $e^{\sqrt{-1\theta}}T(\delta_1 + k\delta_2)T(\delta_1 - k\delta_2)$  where  $\theta$  is the angle between  $\delta_1 + k\delta_2$  and  $\delta_1 - k\delta_2$ . This is an extension to space of a formula of Laguerre.

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## NOTE ON THE POTENTIAL AND THE ANTI-POTENTIAL GROUP OF A GIVEN GROUP.

BY PROFESSOR G. A. MILLER.

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§ 1. Introduction.

WITH every regular substitution group there may be associated a conjugate substitution group on the same letters