

AN ADVANCE IN THEORETICAL MECHANICS.

Théorie des Corps déformables. Par E. COSSERAT et F. COSSERAT. Paris, A. Hermann et Fils, 1909. vi+226 pp.

IN a recent review* of the French edition of the first half of Chwolson's monumental treatise on physics, we purposely and explicitly omitted comment upon two extended notes† of the Cosserats on the foundations of analytical mechanics other than first to state that, owing to the difficulty of the notes themselves and the lack of a general theoretical treatment of mechanics in Chwolson's volumes, these notes seemed out of place, and second to promise that these important contributions of the Cosserats should shortly be reviewed. The *Théorie des Corps déformables* is a reprint, with repagination, of the second of these notes, and may be obtained separately by those who may want it without the rest of Chwolson's highly valuable treatise.

The underlying idea of the Cosserats is to base analytical mechanics, in its most widely extended sense, not upon Newton's laws or Hamilton's principle, but upon what they call *euclidean action*, and to define the common concepts of mechanics in terms of this euclidean action; to develop a general theory which shall include as special cases newtonian mechanics and its various derivatives or extensions, of which there are so many, hydrodynamics, elasticity, and electromagnetism, and which shall extend in its generality to an infinity of possible non-newtonian systems of mechanics, of which at least one is now familiar to students of relativity. This ambitious task they have certainly accomplished, and from the favor in which their work seems to be received by such authorities as Appell, it is by no means impossible that Hamilton's principle, which up to the present has contained the most general and unifying theory of mechanics, may rapidly become replaced by the Cosserats' euclidean action.

The fundamental geometric element of their system is not the point, but the point carrying a system of rectangular axes, that is, the trirectangular triedral angle. It is clear that the

* This BULLETIN, volume 18, pp. 497-508, July, 1912.

† Chwolson, *Traité de Physique*, volume 1, pp. 236-273, and volume 2, pp. 953-1173.