

## TOPOLOGICAL DYNAMICS

BY WILLIAM A. VEECH<sup>1</sup>

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**Introduction.** This will be a survey of recent developments in two areas of topological dynamics, "dynamical embedding" (Part 1) and the structure of minimal flows (Part 2). Part 2 contains some results published here for the first time.

#### 1. DYNAMICAL EMBEDDING

Any sequence with values in a topological space or a probability space may be viewed as a "sample sequence" of a (nonunique) dynamical system or

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