

## THE SOLVABILITY OF THE CONJUGACY PROBLEM FOR CERTAIN HNN GROUPS

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**1. Introduction.** Let  $B$  be a free product of finitely generated free groups with infinite cyclic amalgamated subgroups. It is well known that  $B$  has a solvable conjugacy problem [12]. Suppose  $B$  is given by

$$\langle b_1, \dots, b_n, c_1, \dots, c_m; R(b_1, \dots, b_n) = S(c_1, \dots, c_m) \rangle,$$

and let  $W$  and  $V$  be words in the generators of  $B$  defining nonidentity elements of the same order. Let  $G$  be the HNN group in the sense of [11] given by

$$\langle a, b_1, \dots, b_n, c_1, \dots, c_m; R = S, a^{-1}Wa = V \rangle.$$

Here we show

**THEOREM.** *If  $B$  is residually free and 2-free then  $G$  has solvable conjugacy problem.*

Let  $A$  consist of those groups  $B$  given above such that  $m=n$ ,  $S=f(R)$ , where  $f: \langle b_1, \dots, b_n \rangle \rightarrow \langle c_1, \dots, c_n \rangle$  is an isomorphism and  $R$  generates its own centralizer in its factor. From [5] and our theorem we obtain

**COROLLARY 1.** *If  $B$  is in  $A$  then  $G$  has solvable conjugacy problem.*

As a consequence we obtain a result known to a number of workers in this area:

**COROLLARY 2.** *Let  $G$  be a one-relator group given by*

$$\langle a, b_1, \dots, b_k; a^{-1}P(b_1, \dots, b_k)a = Q(b_1, \dots, b_k) \rangle.$$

*Then  $G$  has solvable conjugacy problem.*

Among these groups are the two generator one-relator nonhopfian groups  $G(l, m)$  which have been the subject of a great deal of discussion in recent years [1, 2, 3, 5, 6, 15]. For concepts and terminology the reader should consult [14], [16].

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