

A CHARACTERIZATION OF HOMOGENEOUS PLANE CONTINUA THAT ARE CIRCULARLY CHAINABLE¹

BY C. E. BURGESS

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It has recently been shown independently, with simultaneous announcements, by Fearnley [10] and Rogers [15] that the pseudo-arc [1], [2], [12], [13] is the only nondegenerate homogeneous plane continuum that is both circularly chainable and hereditarily indecomposable. Thus the pseudo-circle, described by Bing [2, p. 48], is not homogeneous. It is the purpose of this note to show that this result by Fearnley and Rogers can be combined with various other theorems to obtain a characterization of all nondegenerate homogeneous plane continua that are circularly chainable. It is interesting that the class of all such continua consists of the three known examples of nondegenerate homogeneous plane continua; namely, the simple closed curve, the pseudo-arc, and the circle of pseudo-arcs [7].

Definitions of *linearly chainable continua* and of *circularly chainable continua* can be found in [8]. In some of the references, continua of the former type have been called *chainable continua* or *snake-like continua*, and those of the latter type have been called *circle-like continua*. With the definitions used here, there exist nondegenerate continua which are both linearly chainable and circularly chainable [8, Theorem 7], but in some places in the literature this is not permitted [5, p. 210]. A continuum M is defined to be *homogeneous* if for each two points x and y of M there is a homeomorphism of M onto itself that takes x onto y .

It is our intention to include enough references to indicate a complete proof of the following theorem, even though some parts of the proof may already be known to people who are familiar with the references. A history of work on the problem of classifying homogeneous plane continua can be found in [7].

THEOREM. *A nondegenerate circularly chainable plane continuum is homogeneous if and only if it is either a simple closed curve, a pseudo-arc, or a circle of pseudo-arcs.*

PROOF. A pseudo-arc has been characterized by Bing [2] as a linearly chainable continuum that is hereditarily indecomposable. Bing

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