

by identifying the surface with the functional obtained by integrating  $k$ -forms over the surface.

One of the most important features of the space of varifolds is a certain compactness property which makes it possible to obtain a varifold as a "weak" solution to Plateau's problem. While the local structure of such solutions is not yet completely known, the author states some theorems valid for two-dimensional varifolds in Euclidean three space,  $R^3$ , that improve upon the results of T. Rado and J. Douglas concerning least area problems. Perhaps the most interesting is the one that combines the results of W. H. Fleming and E. R. Reifenberg and which states that if a boundary  $C$  is prescribed which is the union of a finite number of disjoint simple closed smooth curves in  $R^3$ , then there is a two-dimensional varifold  $V$  which is a solution to this problem and has the property that the support of  $V$  minus the points of  $C$  is a two-dimensional real analytic manifold. The beauty of this solution comes from the fact that varifolds include all smooth surfaces and thus the solution  $V$  represents a surface of least area among all competing surfaces and not merely one of least area among those of prescribed topological type.

This book consists of four chapters, the last two of which describe varifolds and variational problems involving varifolds. In order to set the stage for this discussion, the first chapter gives an interesting expository account of least area phenomena and the second deals with the subject of rectifiable subsets of Euclidean space. A  $k$ -dimensional rectifiable set is one which can be approximated (in the sense of  $k$ -dimensional Hausdorff measure) by smooth  $k$ -manifolds. Rectifiable sets have become objects of fundamental importance to measure theoretic geometry since they are essential in describing the structure of sets of finite  $k$ -dimensional Hausdorff measure.

The material in this book is designed to be accessible to students who had a solid course in advanced calculus and it would serve nicely as a supplement to a course in the calculus of variations. The numerous revealing examples, which are accompanied by illustrations, will enable the reader to obtain a strong intuitive grasp of the many intricacies that are associated with Plateau's problem.

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*Lie theory and special functions* by Willard Miller, Jr. Mathematics in Science and Engineering, vol. 43, Academic Press, New York, 1968. xv+338 pp. \$16.50.

The principal aim of this book is to provide a group-theoretic interpretation of certain properties of the special functions of math-