

RESEARCH ANNOUNCEMENTS

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ON THE FACTORIZATION OF A CLASS OF DIFFERENCE OPERATORS¹

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Communicated by Wolfgang Wasow, June 19, 1968

The differential equation for the Meijer G -function (generalized hypergeometric function) with respect to the argument z , [1], can be written in an elegant factored form using the differential operator $z(d/dz)$. Recently, [2], [3], it has been found that particular Meijer G -functions satisfy difference equations with respect to a parameter, and it is the purpose of this paper to deduce analogous factored forms for these difference equations.

Consider the function

$$(1) \quad G(x) = \frac{1}{2\pi i} \int_L z^s \Omega(s) K(s, x, y) ds,$$

$$(2) \quad \Omega(s) = \frac{\Gamma(c-s) \prod_{j=1}^m \Gamma(b_j-s) \Gamma(1-c+s) \prod_{j=1}^k \Gamma(1-a_j+s)}{\prod_{j=m+1}^q \Gamma(1-b_j+s) \prod_{j=k+1}^p \Gamma(a_j-s)},$$

$$0 \leq m \leq q, \quad 0 \leq k \leq p; \quad a_j \neq b_i, \quad 1 \leq j \leq k, \quad 1 \leq i \leq m,$$

$$(3) \quad K(s, x, y) = \Gamma(x + \delta s) / \Gamma(x + y + \epsilon s), \quad \epsilon \text{ and } \delta \text{ integers, } \delta \geq 0,$$

where L is an infinite loop contour which separates the poles of $\Gamma(x + \delta s) \cdot \Gamma(1-c+s) \prod_{j=1}^k \Gamma(1-a_j+s)$ from those of $\Gamma(c-s) \prod_{j=1}^m \Gamma(b_j-s)$. Here and in what follows, we tacitly assume that the complex quan-

¹ This work was supported by the United States Atomic Energy Commission under Contract No. AT(11-1)1619.