

It is worthwhile noting that the logarithm of the outer factor $p^*g(p)$ exists, and is uniquely determined by the magnitudes of the f_n on the boundary, since $\log p^*g(p)$ are uniquely determined by $\log |f_n(\omega)|$.

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THREE THEOREMS ON MANIFOLDS WITH BOUNDED MEAN CURVATURE

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The following are three theorems about manifolds having bounded mean curvature which illustrate some of the applications to classical differential geometry of the structure theorems for regular integral varifolds. The proofs, which will appear in [A], are geometric and measure theoretic. Let $2 \leq k \leq n$ be integers.

THEOREM 1. *There exist numbers $a(k) > 0$ and $b(k, n) < \infty$ with the following property: Let A be a compact k -dimensional manifold of class C^2 with boundary B and $f: A \rightarrow R^n$ be a C^2 immersion of A into R^n having mean curvature no larger than M at each point. If*

$$M^k [k\text{-area of } f|A] \leq a(k),$$

then

$$[k\text{-area of } f|A] \leq b(k, n) [(k-1)\text{-area of } f|B]^{k/(k-1)}.$$

In particular, if f satisfies the minimal surface equation, then, without additional hypotheses,