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ISOMORPHIC COMPLEXES

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In this paper we show that if K and L are n -complexes, then K and L are isomorphic iff the 1-sections of the first derived complexes of K and L are isomorphic. This provides a low-dimensional method for establishing the isomorphism (homeomorphism) of complexes (polyhedra).

Throughout, s_p will denote a (rectilinear) p -simplex with vertices a^0, a^1, \dots, a^p ; K will denote a (finite geometric) complex with n -section K^n and first derived complex K^1 . The *closed star* of a vertex a of K , $st(a)$, is the set of simplexes of K having a as a face and all their faces. For more details see [2].

DEFINITION 1. An n -complex K is *full* provided, for any subcomplex L of K which is isomorphic to s_p^1 , $2 \leq p \leq n$, L^0 spans a p -simplex of K .

THEOREM 1. *Suppose K and L are full n -complexes. Then K and L are isomorphic iff K^1 and L^1 are isomorphic.*

PROOF. We need only consider the case when K^1 and L^1 are isomorphic. Let $v: K^1 \rightarrow L^1$ be an admissible vertex transformation of K^1 onto L^1 with an admissible inverse. Then a^0, a^1 span a 1-simplex of K iff $v(a^0), v(a^1)$ span a 1-simplex of L . Furthermore, for any p , $2 \leq p \leq n$, if a^0, a^1, \dots, a^p span a p -simplex s_p of K , then $v[s_p^1]$ is isomorphic to s_p^1 . So, using the fullness of L , we get that $(v[s_p^1])^0$