

## TOPOLOGY

99. C. L. Clark: *Arc reversing transformations.*

If  $A$  and  $B$  are separable metric spaces,  $B$  nondegenerate, a single-valued continuous transformation  $f(A) = B$  is said to be arc reversing provided the inverse of every simple arc in  $B$  is a simple arc in  $A$ . After several basic results are obtained, it is shown that if  $f(A) = B$  is arc reversing, with  $A$  locally compact and  $B$  a locally connected generalized continuum, then the sets  $A - A_1$  and  $B - B_1$  are homeomorphic, where  $B_1$  is the set of all points  $b$  in  $B$  whose inverses  $f^{-1}(b)$  are nondegenerate and  $A_1 = f^{-1}(B_1)$ . In particular if  $f(A) = B$  is (1-1),  $A$  and  $B$  are homeomorphic. A characterization of arc reversing transformations is afforded by the result that a single-valued continuous transformation  $T(A) = B$ , where  $A$  and  $B$  are locally connected continua, is arc reversing if and only if the set of inverses  $[T^{-1}(b)]$ ,  $b$  in  $B$ , consists of single points and at most a countable number of free arcs whose end points are of Urysohn-Menger order at most 2 in  $A$ . Further results are obtained concerning local separating points and continua having homeomorphs of finite linear measure. (Received December 29, 1943.)

100. Mariano García: *Component orbits under pointwise recurrent homeomorphisms.*

A point  $x$  of a separable metric space  $X$  on which a homeomorphism  $f(X) = X$  is defined is called recurrent under  $f$  if, given any neighborhood  $U$  of  $x$ , there exists an  $N$  such that  $f^N(x) \in U$ , and an invariant set  $L$  in  $X$  whose components can be ordered in a sequence  $\dots, A_{-2}, A_{-1}, A_0, A_1, A_2, \dots$  such that  $f(A_i) = A_{i+1}$  is defined as a component orbit. Using methods analogous to those used by Whyburn in proving the results that Hall and Schweigert obtained relative to periodic component orbits (component orbits having a finite number of components) under a pointwise periodic homeomorphism on  $X$ , this paper establishes extensions of these results to non-pointwise periodic mappings. It is shown for example that if  $f(X) = X$  is a homeomorphism on a compact space  $X$  and  $G_1, G_2, \dots$  is a sequence of component orbits whose limit inferior contains a periodic component orbit  $Q$ , and if (either) each point of  $\limsup G_i - Q$  is recurrent under both  $f$  and  $f^{-1}$  or each point of  $\sum_{i=1}^{\infty} G_i + \limsup G_i$  is recurrent under  $f$ , then  $\limsup G_i$  is a periodic component orbit. (Received December 27, 1943.)

101. W. H. Gottschalk: *Powers of homeomorphisms with almost periodic properties.*

Let  $X$  be a topological space and let  $f(X) = X$  be a homeomorphism. A point  $x$  of  $X$  is said to be recurrent under  $f$  provided that to each neighborhood  $U$  of  $x$  there corresponds a positive integer  $n$  such that  $f^n(x) \in U$ . A point  $x$  of  $X$  is said to be almost periodic under  $f$  provided that to each neighborhood  $U$  of  $x$  there corresponds a monotone increasing sequence  $n_1, n_2, \dots$  of positive integers with the properties that the numbers  $n_{i+1} - n_i$  ( $i = 1, 2, \dots$ ) are uniformly bounded and  $f^{n_i}(x) \in U$  ( $i = 1, 2, \dots$ ). A subset  $Y$  of  $X$  is said to be minimal under  $f$  provided that  $Y$  is nonvacuous, closed and invariant under  $f$ , and furthermore  $Y$  does not contain a proper subset with these properties. The following theorems are established: (1) If  $x \in X$  is recurrent under  $f$ , then  $x$  is also recurrent under  $f^n$  for every positive integer  $n$ . (2) If  $X$  is minimal under  $f$  but not under  $f^k$ , where  $k$  is a nonzero integer, then there exists an integer  $n$ ,  $n > 1$ , such that  $n$  divides  $|k|$  and  $f^n$  gives a finite minimal-set decomposition of  $X$  which