

FURTHER NON-INVOLUTORIAL CREMONA SPACE  
TRANSFORMATIONS CONTAINED IN A SPECIAL  
LINEAR COMPLEX\*

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1. *Introduction.* In a series of papers by Snyder,† Carroll,‡,§ and the author, ||, ¶ involutorial transformations were defined by means of a correspondence between the surfaces of a pencil and the points of a rational curve. The purpose of this paper is to apply similar methods to certain non-involutorial transformations.

2. *Definition of the Transformation.* Given a line  $d$  and two pencils of surfaces  $|F_n|$  and  $|F_{n'}|$  of orders  $n$  and  $n'$  which contain  $d$  as an  $(n-1)$ -fold and  $(n'-1)$ -fold line, respectively. Make the surfaces of each pencil projective with the points of  $d$ . A point  $P$  will determine a unique surface  $F_n$  passing through it, hence a unique point  $O$  on  $d$  and a unique surface  $F_{n'}$ . The line  $PO$  cuts  $F_{n'}$  in one point  $P'$  (other than  $O$ ) which is defined as the image of  $P$ .

Since  $P$  and  $P'$  lie on a line which intersects  $d$ , any plane through  $d$  is transformed into itself. We shall find the plane transformation in an arbitrary plane through  $d$  and then generate the space transformation by revolving the plane about  $d$ .

3. *The Plane Transformation.* The intersections of an arbitrary

\* Presented to the Society, December 27, 1933.

† Virgil Snyder, *On a series of involutorial cremona transformations of space defined by a pencil of ruled surfaces*, Transactions of this Society, vol. 35 (1933), pp. 341-347.

‡ Evelyn Carroll, *Systems of involutorial birational transformations contained multiply in special linear line complexes*, American Journal of Mathematics, vol. 54 (1932), pp. 707-717.

§ Evelyn Carroll-Rusk, *Cremona involutions defined by a pencil of cubic surfaces*, American Journal of Mathematics, vol. 56 (1934), pp. 96-108.

|| Amos Black, *Types of involutorial space transformations associated with certain rational curves*, Transactions of this Society, vol. 34 (1932), pp. 795-810.

¶ Amos Black, *Types of involutorial space transformations associated with certain rational curves—composite basis curves*, this Bulletin, vol. 40 (1934), pp. 417-420.