

\mathfrak{B}^m . The system of neighborhoods \mathfrak{B}^m for fixed m covers Ω and may be replaced by a finite subsystem,

$$\mathfrak{B}^{m_1}, \mathfrak{B}^{m_2}, \dots, \mathfrak{B}^{m_k};$$

such that each point of Ω is interior to some class \mathfrak{B}^{m_k} and each class \mathfrak{B}^{m_k} is a neighborhood of a point Q^{m_k} of the class Ω . Let \mathfrak{C} be the class of all points Q^{m_k} . Since every point P of Ω is interior to some set \mathfrak{B}^{m_k} , it follows from condition (4) that Q^{m_k} is contained in the neighborhood \mathfrak{B}^m of P . Therefore P is a limiting point of the class \mathfrak{C} .

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This article was in type before the writer learned of the existence of an article by Fréchet (*Bulletin de la Société mathématique de France*, volume 35, 1917), in which it is shown that the closure of derived classes is a consequence of the Heine-Borel property in the case of a general system \mathfrak{L} . Theorem 3 of the present paper is a generalization of this result.

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INTEGRALS AROUND GENERAL BOUNDARIES.

BY PROFESSOR P. J. DANIELL.

THE concept of a boundary integral has been extended to curves of the type $x = x(t)$, $y = y(t)$, where $x(t)$, $y(t)$ are absolutely continuous functions of a parameter t . In this case the curves are more or less simple and have tangents "nearly everywhere." In applications to physics however the boundary must be considered rather as a boundary of a set (in the sense of the theory of point sets). The boundary will be, in general, a collection of points without definite tangents at all. This paper sets out a method by which such boundary integrals can be defined under certain restrictions placed on the two integrand functions u , v . The method depends on the concept of absolutely additive functions of sets.* The writer believes that these restrictions could be lightened and that there is a wide field here for further investigation.

* J. Radon, *Wiener Sitzungsberichte*, vol. 122 (1913), p. 1295. W. H. Young, *Proceedings London Math. Society*, vol. 13 (1914), p. 109.