

3 sextactic points are contacts of tangents from the flexes P_3 . The 6 contacts of tangents from the sextactic points are the points P_{12} . The 12 contacts of tangents from P_{12} in turn are the points P_{24} , and so on ad infinitum.

UNIVERSITY OF OREGON.

RELATED INVARIANTS OF TWO RATIONAL SEXTICS.

BY PROFESSOR J. E. ROWE.

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LET the parametric equations of the R_3^6 , the rational curve of order six in three dimensions, be

$$(1) \quad x_i = \delta_{it}^6 \equiv a_i t^6 + 6b_i t^5 + 15c_i t^4 + 20d_i t^3 + 15e_i t^2 + 6f_i t + g_i \quad (i = 1, 2, 3, 4),$$

and let the parametric equations of the R_2^6 , the rational plane curve of order six, be of the form

$$\begin{aligned} x_1 &= \alpha_t^6 \equiv a + bt + ct^2 + dt^3 + et^4 + ft^5 + gt^6, \\ x_2 &= \beta_t^6 \equiv a' + b't + c't^2 + d't^3 + e't^4 + f't^5 + g't^6, \\ x_3 &= \gamma_t^6 \equiv a'' + b''t + c''t^2 + d''t^3 + e''t^4 + f''t^5 + g''t^6. \end{aligned}$$

It is well known that all plane sections of the R_3^6 are apolar to a doubly infinite system of binary sextics, and that all line sections of the R_2^6 are apolar to a triply infinite system of binary sextics. We shall let the four binary sextics δ_{it}^6 of (1) be four linearly independent sextics of the apolar system of the R_2^6 , and the $\alpha_t^6, \beta_t^6, \gamma_t^6$ of (2) be three linearly independent sextics of the apolar system of the R_3^6 . Our purpose is to point out briefly the relation between the invariants of the R_2^6 and the invariants* of the R_3^6 .

By means of the twelve equations

* This relation must not be confused with the correspondence between invariants of the R_2^n and covariant surfaces of the R_3^n .