

conics. The author states for example that every plane quintic can be regarded as conjugate to a line in an involution determined by a net of cubics, having a suitable number of fundamental points.

11. By the aid of parametric representation of the points on a non-singular plane cubic, Professor Emch discusses the collinearity of the 27 points of contact of tangents to the cubic from its 9 inflexions. He finds 81 lines containing each 3 such points, and 81 other lines connecting 2 contact points with an inflexion.

12. Professor Halsted gave a brief outline of "intrinsic spherics", or spherical trigonometry independent of the parallel postulate, and advocated from a pedagogical standpoint the introduction of the sphere as two-dimensional figure into elementary geometry, instead of the use of the three-dimensional globe.

13. The problem of determining all algebraic minimal surfaces was solved analytically by Weierstrass in 1866 (see his collected works, volume 3, pages 39-52). Darboux, in his *Théorie générale des surfaces*, part 1, No. 221, has shown that such surfaces can always be generated by the translation of an algebraic curve. This shows that the function $F(s)$ used in the formulas of Weierstrass must be algebraic. Professor Hancock proposes as a problem next to be attacked the question of determining all those minimal surfaces which are not themselves algebraic, but contain a sheaf of algebraic curves.

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ON THE USE OF HYPERCOMPLEX NUMBERS IN CERTAIN PROBLEMS OF THE MODULAR GROUP.

BY DR. J. W. YOUNG.

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THE following discussion connects two subjects which have hitherto been considered apart, and indicates a method of attacking certain modular group problems which seems susceptible of further elaboration.