

# BPS microstates and the open topological string wave function

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## Abstract

It has recently been conjectured that the closed topological string wave function computes a grand canonical partition function of Bogomol'nyi–Prasad–Sommerfield (BPS) black hole states in four dimensions:  $Z_{\text{BH}} = |\psi_{\text{top}}|^2$ . We conjecture that the open topological string wave function also computes a grand canonical partition function, which sums over black holes bound to BPS excitations on D-branes wrapping cycles of the internal Calabi–Yau:  $Z_{\text{BPS}}^{\text{open}} = |\psi_{\text{top}}^{\text{open}}|^2$ . This conjecture is verified in the case of Type IIA on a local Calabi–Yau three-fold involving a Riemann surface, where the degeneracies of BPS states can be computed in  $q$ -deformed two-dimensional Yang–Mills theory.