## 92. On the Structure of Certain Types of Polarized Varieties. II

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This is a continuation of our previous notes [1], [2]. We employ the same notation and the same terminology as in them. We shall outline our main results. Details will be published elsewhere.

1. Polarized varieties with  $\Delta = 0$ . Given a pair (x, y) of points on a projective space P, we denote by  $l_{x,y}$  the line which passes through the points x and y. Given a pair (X, Y) of subsets of P, we denote by  $X^*Y$  the subset  $(\bigcup_{(x,y)\in X\times Y, x\neq y^{i}x,y})\cup X\cup Y$  of P.

Theorem 1. i) Let (V, F) be a polarized variety with  $\Delta(V, F) = 0$ . Then V is normal and F is very ample.

ii) Let  $\rho: V \to \mathbf{P}^N$  be the embedding associated with F, and let S be the set of singular points of V. Then S is a linear subspace of  $\mathbf{P}^N$ .

iii) Let L be a linear subspace of  $\mathbf{P}^N$  such that dim  $L + \dim S = N$ -1 and  $L \cap S = \emptyset$ . Put  $V_L = V \cap L$ . Then  $V_L$  is non-singular,  $\Delta(V_L, F)$ =0 and  $V = V_L^*S$ .

**Remark.** By this theorem the classification of polarized varieties with  $\Delta = 0$  is reduced to that of non-singular ones. Recall that an enumeration of such polarized manifolds has already been given in [1].

2. Families of polarized varieties with  $\Delta = 0$ . Theorem 2. Let  $\pi: CV \rightarrow T$  be a proper, flat morphism from a variety V to another variety T, which may not be compact. Suppose that for every  $t \in T$  the fiber  $V_t = \pi^{-1}(t)$  is irreducible and reduced. Let F be a line bundle on CV which is relatively ample to  $\pi$ . Suppose that  $\Delta(V_0, F_0) = \Delta(V_0, F_{V_0}) = 0$  for some  $0 \in T$ . Then  $\Delta(V_t, F_t) = 0$  for any  $t \in T$ .

Corollary 2.1. Suppose in addition that  $d(V_0, F_0) = 1$ . Then  $\subseteq \mathcal{V}$  is a  $P^n$ -bundle over T.

Corollary 2.2. Suppose in addition that  $d(V_0, F_0)=2$ . Then there exists an embedding  $\mathbb{C}V \to \mathbb{P}$  where  $\mathbb{P}$  is a  $P^{n+1}$ -bundle over T. Moreover  $\mathbb{C}V$  is a divisor on  $\mathbb{P}$  and  $V_t$  is a quadric in  $P_t \cong P^{n+1}$  which is the fiber of  $\mathbb{P} \to T$  over  $t \in T$ .

Corollary 2.3. Suppose in addition that  $d(V_0, F_0) \ge 3$ , that  $V_0$  is non-singular and that the canonical bundle of  $V_0$  is a restriction of a line bundle on  $\bigcirc V$ . Then every fiber  $V_t$  is non-singular. Moreover, except the case in which  $\bigcirc V$  is a  $P^2$ -bundle over T, there exists a  $P^1$ -