

ERRATA: PRINCIPAL SERIES WHITTAKER FUNCTIONS ON $Sp(2; \mathbf{R})$, II

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This is the correction of our paper cited in the title.

Let $\pi(P_1; (\varepsilon, D_k^-); \nu_1 + \rho_{P_1})$ be a principal series representation of odd type considered in Proposition 2.1 (ii). The cause of mistake is that the corner K -type of this representation was wrongly specified; namely in the page 248, we should read “ $\max(\lambda_2, k)$ ” as “ λ_2 ” in the line 2 and “ $\tau_{(l, l-1)}$ (resp. $\tau_{(l, -k-1)}$)” as “ $\tau_{(l+1, l)}$ (resp. $\tau_{(l+1, -k)}$)” in the line 6.

On the second line in Section 7, $\tau_{(k+1, k)}$ should be replaced by $\tau_{(k, k-1)}$. Therefore the down shift operator $\mathcal{E}_k^{\text{down}}$ in Subsection 7.2 should read

$$\mathcal{E}_k^{\text{down}} : C_{\eta, (k, k-1)}^\infty(N \backslash G/K) \rightarrow C_{\eta, (k-1, k-2)}^\infty(N \backslash G/K).$$

We have to replace the following Definition 7.2 by

$$c_i(a) = a_1^{k+2-i} a_2^{k-i} e^{-\sqrt{-1}\eta_{2e_2} a_2^2} h_i(a), \quad i = 0, 1.$$

Then the functions h_i satisfy the following equations:

- (i) $\eta_{e_1-e_2} a_1^2 h_0(a) + \partial_1 h_1(a) = 0,$
- (ii) $a_2^2 \partial_2 h_0(a) + \eta_{e_1-e_2} h_1(a) = 0,$
- (iii) $((\partial_1 + \partial_2)^2 + 2k(\partial_1 + \partial_2) - 4\sqrt{-1}\eta_{2e_2} a_2^2 \partial_2) h_0(a) = (v_1^2 - k^2) h_0(a),$
- (iv) $((\partial_1 + \partial_2)^2 + 2(k-2)(\partial_1 + \partial_2) - 4\sqrt{-1}\eta_{2e_2} a_2^2 \partial_2) h_1(a) = (v_1^2 - (k-2)^2) h_1(a).$

From the equations (i) and (ii), we obtain

$$\left(\partial_1 \partial_2 - \eta_{e_1-e_2}^2 \left(\frac{a_1}{a_2} \right)^2 \right) h_i(a) = 0$$

for $i = 0, 1$. We introduce the integral transforms

$$h_i(a) = \int_{\mathbf{R}} \phi_i(u) \exp \left\{ c \left(\frac{u}{a_2^2} - \frac{\eta_{e_1-e_2}^2}{4u} a_1^2 \right) \right\} \frac{du}{u},$$

and put $\phi_0(u) = v^{-1/2-k} \psi_0(v)$ and $\phi_1(u) = v^{-1/2-k+2} \psi_1(v)$ with $v = \sqrt{u}$. Then we see that those satisfy

$$v^2 \frac{d^2 \psi_i}{dv^2} + \left(\frac{1}{4} - v_1^2 - 8\sqrt{-1}\eta_{2e_2} v^2 \right) \psi_i = 0$$