CORRIGENDUM TO: ON THE EXCEPTIONAL SET OF HARDY-LITTLEWOOD'S NUMBERS IN SHORT INTERVALS

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Let $k \ge 2$ be an integer. In the paper [1] we proved a result on the set E_k of the integers which are neither a sum of a prime and a k-power nor a k-power of an integer. Setting $E_k(X) = E_k \cap [1, X]$ and $E_k(X, H) = E_k \cap [X, X + H]$, where X is a sufficiently large parameter and H = o(X), our statement is

THEOREM. Let $k \ge 2$ be a fixed integer and $K = 2^{k-2}$. There exists a (small) positive absolute constant δ such that for $H \ge X^{7/12(1-1/k)+\delta}$

$$|E_k(X,H)| \ll H^{1-\delta/(5K)}$$
.

In fact our proof is not totally correct. There are two corrections to do. The first one is that the level Q of the the Farey dissection has to be fixed equal to $2kY^{1-1/k}$ instead of $4Y^{1-1/k}$ since, in the proof of Lemma 10 of [1], such a condition is needed to estimate, by using the first derivative method, the order of magnitude in a Farey arc of

$$F_k(\alpha) = \sum_{Y/4 \le m^k \le Y} e(m^k \alpha),$$

where $Y = X^{7/12+10\delta+\epsilon}$ and $e(\alpha) = e^{2\pi i\alpha}$. We write here the corrected version of Lemma 10 of [1] whose proof is a slight modification of what Perelli-Zaccagnini [3], eq. (39)–(40), proved.

LEMMA 10 OF [1]. Let (a,q) = 1, $Q \ge 2kY^{1-1/k}$ and $|\eta| \le 1/qQ$. Then

$$\left| F_k \left(\frac{a}{q} + \eta \right) \right| \ll \frac{Y^{1/k-1}}{|\eta|}.$$