On some mixed problems for fourth order hyperbolic equations

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§1. Introduction and statement of result

We consider some mixed problems for fourth order hyperbolic equations. Let S be a smooth and compact hypersurface in \mathbb{R}^n $(n \ge 2)$ and \mathcal{Q} be the interior or exterior of S. Let

(E)
$$Lu + Bu = \left(\frac{\partial^4}{\partial t^4} + (a_1 + a_2 + a_3)\frac{\partial^2}{\partial t^2} + a_3a_1\right)u + B\left(x, t, \frac{\partial}{\partial t}, D\right)u$$

= $f(x, t)$

Here $a_k(k=1, 2, 3)$ are the following operators:

(1.1)
$$a_{k} = -\sum_{i,j}^{n} \frac{\partial}{\partial x_{i}} \left(a_{k,ij}(x) \frac{\partial}{\partial x_{j}} \right) + b_{k}(x, D).$$
$$a_{k,ij}(x) = a_{k,ji}(x)$$

are real,

$$\sum_{ij}^{n} a_{k,ij}(x) \xi_i \xi_j \geq \delta |\xi|^2, \quad (\delta > 0)$$

for every $(x, \xi) \in \mathcal{Q} \times \mathbb{R}^n$ (k=1, 2, 3). *B* denotes an arbitrary third order differential operator. b_k are first order operators. Let us assume that all coefficients are sufficiently differentiable and bounded in $\overline{\mathcal{Q}}$ or in $\overline{\mathcal{Q}} \times (0, \infty)$. Recently S. Mizohata treated mixed problems for the equations of the form

$$L = \prod_{i=1}^{m} \left(\frac{\partial^2}{\partial t^2} + c_i(x) a(x, D) \right) + B_{2m-1},$$