

RESTRICTION OF THE HOLOMORPHIC COHOMOLOGY OF A SHIMURA VARIETY TO A SMALLER SHIMURA VARIETY

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1. Introduction. Suppose $S = S(\Gamma) = \Gamma \backslash X$ is a *Shimura variety* obtained as the quotient of a Hermitian symmetric space $X = G(\mathbb{R})/K_\infty$ (where G is a semi-

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