

# BOUNDED LINEAR OPERATORS BETWEEN $C^*$ -ALGEBRAS

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**Introduction.** Let  $u: A \rightarrow B$  be a bounded linear operator between two  $C^*$ -algebras  $A, B$ . The following result was proved in [P1].

**THEOREM 0.1.** *There is a numerical constant  $K_1$  such that for all finite sequences  $x_1, \dots, x_n$  in  $A$  we have*

$$(0.1)_1 \quad \max \{ \|(\sum u(x_i)^* u(x_i))^{1/2}\|_B, \|(\sum u(x_i) u(x_i)^*)^{1/2}\|_B \} \\ \leq K_1 \|u\| \max \{ \|(\sum x_i^* x_i)^{1/2}\|_A, \|(\sum x_i x_i^*)^{1/2}\|_A \}.$$

A simpler proof was given in [H1]. More recently, another alternate proof appeared in [LPP]. In this paper we give a sequence of generalizations of this inequality.

The above inequality  $(0.1)_1$  appears as the case of “degree one” in this sequence. The next case of degree 2 seems particularly interesting, and so we now formulate it explicitly.

Let us assume that  $A \subset B(H)$  (embedded as a  $C^*$ -subalgebra) for some Hilbert space  $H$ , and similarly that  $B \subset B(K)$ . Let  $(a_{ij})$  be an  $n \times n$  matrix of elements of  $A$ . We define

$$[(a_{ij})]_{(2)} = \max \{ \|(a_{ij})\|_{M_n(A)}, \|(a_{ij}^*)\|_{M_n(A)}, \|(\sum_{ij} a_{ij}^* a_{ij})^{1/2}\|_A, \|(\sum_{ij} a_{ij} a_{ij}^*)^{1/2}\|_A \}.$$

Then we have the following result:

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