# MONODROMY OF THE HYPERGEOMETRIC DIFFERENTIAL EQUATION OF TYPE (3, 6), I 

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To Professor Joji Kajiwara on his sixtieth birthday

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8. Introduction. Fix positive integers $r$ and $n(\geqslant r+1)$, and complex numbers $\alpha_{1}, \ldots, \alpha_{n}$ such that

$$
\alpha_{1}, \ldots, \alpha_{n}, \quad \alpha_{1}+\cdots+\alpha_{n} \notin \mathbb{Z} .
$$

Let $L_{j}(1 \leqslant j \leqslant n)$ be linear forms in $t=\left(t_{0}=1, t_{1}, \ldots, t_{r}\right) \in \mathbb{C}^{r}$ :

$$
L_{j}=\sum_{i=0}^{r} x_{i j} t_{i},
$$

where $x=\left(x_{i j}\right)$ are complex variables such that any $(r+1) \times(r+1)$ minor of the matrix

$$
\left(\begin{array}{cccc}
1 & x_{01} & \cdots & x_{0 n} \\
0 & x_{11} & \cdots & x_{1 n} \\
\vdots & \vdots & \cdots & \vdots \\
0 & x_{r 1} & \cdots & x_{r n}
\end{array}\right)
$$

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