

CERTAIN PERIODIC SEQUENCES OF LAPLACE OF PERIOD SIX IN ORDINARY SPACE

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If a one-to-one point correspondence is established between two surfaces (\mathbf{M}) , (\mathbf{M}') in ordinary space, there exists a net of lines upon each surface called a d-net whose tangents intersect the corresponding tangents of corresponding lines on the other surface. In the present paper we shall discuss the corresponding d-nets which are asymptotic on (\mathbf{M}) and conjugate on (\mathbf{M}') , in short a-c d-nets.

Given an arbitrary surface (\mathbf{M}) , there is a family of surfaces (\mathbf{M}') depending on four arbitrary functions of a variable; each surface (\mathbf{M}') is in point correspondence with (\mathbf{M}) whose d-nets are asymptotic upon (\mathbf{M}) and conjugate upon (\mathbf{M}') . The developables of the congruence $(\mathbf{M}\mathbf{M}')$ correspond to the asymptotics of (\mathbf{M}) .

To a given surface (\mathbf{M}) corresponds a family of congruences $(\mathbf{M}\mathbf{M}')$ depending on two arbitrary functions of one variable; each congruence is conjugate to the asymptotics of (\mathbf{M}) and sustains a family of (\mathbf{M}') depending on two arbitrary functions of a variable.

Given an arbitrary surface (\mathbf{M}') there exists a family of conjugate d-nets depending on four arbitrary functions of one variable whose corresponding d-nets are asymptotic.

If the points of intersection of the corresponding tangents of two d-nets are the foci \mathbf{M}_1 , \mathbf{M}_2 of conjugate tangents $\mathbf{M}'\mathbf{M}_1$, $\mathbf{M}'\mathbf{M}_2$, the corresponding rays $\mathbf{M}\mathbf{M}'$, $\mathbf{M}_1\mathbf{M}_2$ are reciprocal polar lines with respect to the Darboux quadrics at the point \mathbf{M} of (\mathbf{M}) . The d-net of (\mathbf{M}') is harmonic (see [2]). If the points \dots , \mathbf{M}_1^* , \mathbf{M}_2 , \mathbf{M}' , \mathbf{M}_1 , \mathbf{M}_2^* , \dots describe the focal surfaces of the Laplace sequence with respect to the harmonic d-net of (\mathbf{M}') , the points \mathbf{M}_1^* , \mathbf{M}_1 are situated on the asymptotic tangent $\mathbf{M}\mathbf{M}_1$ of (\mathbf{M}) ; \mathbf{M}_2 , \mathbf{M}_2^* on the asymptotic tangent $\mathbf{M}\mathbf{M}_2$.

The above mentioned surfaces form a family depending on six arbitrary functions of one variable. To each surface (\mathbf{M}) of this family there corresponds one and only one surface (\mathbf{M}') , but there exists a family of surfaces (\mathbf{M}) depending on four arbitrary functions of a variable such that to each surface (\mathbf{M}) there correspond two surfaces (\mathbf{M}') , $(\mathbf{M}^{*'})$.

The sequence of Laplace with respect to the d-nets of (\mathbf{M}') , $(\mathbf{M}^{*'})$ coincide,

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