CORRECTION

A CENTRAL LIMIT THEOREM FOR STATIONARY PROCESSES AND THE PARAMETER ESTIMATION OF LINEAR PROCESSES

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Assumptions (i) and (ii) of Theorem 2.1 are insufficient to guarantee the central limit theorem. For the theorem to be valid, a Lindeberg-type or a related condition is needed. Hosoya (1992) used a Lindeberg-type condition and Findley and Wei (1992) proposed a Liapounov-type condition as an additional assumption to the theorem [Findley communicated to us about the error in our assumptions].

Specifically, a version of correction according to the approach of Hosoya (1992) is given as follows.

1. Condition (i) of Lemma A2.4 should be

$$\lim_{m \to \infty} \frac{1}{n(m)} \sum_{k=1}^{n(m)} E \left[u_m(k)^2 I \{ |u_m(k)| \ge \varepsilon n(m)^{1/2} \} \right] = 0.$$

- **2.** Theorem 2.1 (page 134) should have the following additional assumption:
 - (iii) For any $\varepsilon>0$, there exists $B_{\varepsilon}>0$ such that uniformly in N and r

$$E[S(N,r)^{2}I\{S(N,r)>B_{\varepsilon}\}]<\varepsilon,$$

where
$$S(N,r) = [\sum_{\alpha=1}^{p} \{\sum_{t=1}^{N} x_{\alpha}(t+r)/N^{1/2}\}^{2}]^{1/2}$$
.

3. The line which contains (6.18) in the proof (pages 146 and 147) should be deleted and the following lines should be added after the last line of the proof:

It holds that

$$\begin{split} E\Big\{ & \left(\eta_k - E\big(\eta_k | \mathscr{F}_{k-1}^*\big) \right)^2 I \big(\big| \eta_k - E\big(\eta_k | \mathscr{F}_{k-1}^*\big) \big| > 2B_{\varepsilon} \big) \Big\} \\ & \leq 2 E\Big\{ \eta_k^2 I \big(\big| |\eta_k| - \big| E\big(\eta_k | \mathscr{F}_{k-1}^*\big) \big| \big| > 2B_{\varepsilon} \big) \big\} + 2 E\Big\{ E\big(\eta_k | \mathscr{F}_{k-1}^*\big)^2 \Big\} \\ & \leq 2 E\Big\{ \eta_k^2 I \big(|\eta_k| > B_{\varepsilon} \big) \big\} + 2 E\Big\{ \eta_k^2 I \big(\big| E\big(\eta_k | \mathscr{F}_{k-1}^*\big) \big| > B_{\varepsilon} \big) \big\} \\ & + 2 E\Big\{ E\big(\eta_k | \mathscr{F}_{k-1}^*\big)^2 \Big\}, \end{split}$$

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