CORRECTION AND ADDENDUM

ON EFFICIENT ESTIMATION IN REGRESSION MODELS

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First we have some corrections. The first conclusion of Proposition 5.8 should read

$$egin{aligned} rac{1}{N_n} \sum_{j=1}^n \hat{w}_{n,j} \, \etaig(\hat{arepsilon}_{n,j}ig) &= rac{1}{N_n} \sum_{j=1}^n \hat{w}_{n,j} igg(\eta(arepsilon_{n,j}) + \int \! \etaig(y - \delta_{n,j} ig) - \eta(y) \, dF(y) igg) \ &+ o_{arepsilon}(n^{-1/2}); \end{aligned}$$

the first conclusion of Lemma 10.2 should be $\Sigma_{n,1} = \mathscr{O}_{\xi_n}(N_n^{-1}a_n^{-4}b_n^{-2})$; in Condition S, $\tilde{s}_{n,j,i}$ stands for $\mathbb{E}_{n,i}(\tilde{s}_{n,j})$; in Section 10, interpret $\mathbb{E}_{n,i}(\hat{e}_{n,i})$ and $\mathbb{E}_{n,i}(\hat{e}_{n,i,j})$ as zero if they are not properly defined.

I would like to comment on the assumptions in Theorem 5.3.

REMARK 1. The conclusions of Theorem 5.3 remain valid if (S2) is weakened to

(WS2)
$$S_{n,2} = \sum_{j=1}^{n} \hat{w}_{n,j} \|\hat{s}_{n,j} - \tilde{s}_{n,j}\|^2 = o_{\xi_n}(1).$$

Indeed, (S2) is only used on page 1519 to conclude that $(\mathbb{E}_n(|C_{n,a}|))^2 = o_{\xi_n}(n^{-1})$, a=1,2; but a similar argument using (WS2) shows that $C_{n,a}^2 = o_{\xi_n}(n^{-1})$, a=1,2, which is all that is needed.

REMARK 2. In addition, (S0) can be relaxed at the expense of a stronger version of Condition R. More precisely, the conclusions of Theorem 5.3 remain valid if (R1) and (R3) are strengthened to

$$(\mathrm{UR1}) \qquad \tilde{R}_{n,1} = \max_{1 \leq j \leq n} \hat{w}_{n,j} \mathbb{E}_n \Big(|\hat{r}_{n,j} - \varrho(Z_j, \, \xi_n)|^2 \Big) = \mathscr{O}_{\xi_n}(n^{-2\alpha}),$$

$$\text{(UR3)} \qquad \tilde{R}_{n,3} = \max_{1 \leq j \leq n} \hat{w}_{n,j} \sum_{i=1}^{n} \mathbb{E}_{n} \Big(|\hat{r}_{n,j} - \hat{r}_{n,j,i}|^{2} \Big) = \mathscr{O}_{\xi_{n}} (n^{-2\alpha}),$$

and (S0) is relaxed to

(WS0)
$$\|\hat{w}_{n,j}\tilde{s}_{n,j}\| \le A_n\hat{w}_{n,j}t_{n,j}, \quad j=1,\ldots,n,$$

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