

The L_∞ -norm of the L_2 -spline projector is bounded independently of the knot sequence: A proof of de Boor’s conjecture

by

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