

STEADY SOLUTIONS OF THE NAVIER-STOKES EQUATIONS REPRESENTING PLANE FLOW IN CHANNELS OF VARIOUS TYPES

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Table of Contents

1. Introduction	
1.1. Background	84
1.2. The boundary-value problem	85
1.3. Channels of various types	87
1.4. Results and methods	89
2. Preliminaries	
2.1. Further notation and terminology	91
2.2. The spaces $H(\Omega)$ and $V(\Omega)$	93
2.3. Identities implied by the conformal map F	95
2.4. Two properties of channels of type II	97
3. Existence of weak solutions	
3.1. A priori bounds	98
3.2. Existence of weak solutions	103
3.3. An a posteriori estimate for weak solutions in channels of type III	104
4. Regularity of the weak solution	108
5. Pointwise decay at infinity for channels of type I'	
5.1. Channels of type I'	109
5.2. Estimates in a boundary neighbourhood	111
5.3. Estimates of the vorticity	114
5.4. Averages over arcs of p and $ p $	117
5.5. Pointwise decay of the pressure and velocity	120
6. Pointwise decay at infinity for channels of type III	
6.1. Introductory remarks	125
6.2. Estimates from the vorticity equation	127
6.3. Decay rates	131

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