

WEIGHTED TRIGONOMETRICAL APPROXIMATION ON R^1 WITH APPLICATION TO THE GERM FIELD OF A STATIONARY GAUSSIAN NOISE

BY

N. LEVINSON and H. P. McKEAN, JR.

Massachusetts Institute of Technology ⁽¹⁾

Contents

1 a. Introduction (weighted trigonometrical approximation)	100
1 b. Introduction (probabilistic part)	101
2. Hardy functions	102
3. Discussion of $Z^- \supset Z^{+/-} \supset Z^- \cap Z^+$	103
4. Discussion of $Z^\bullet$	105
5. Proof of $Z^\bullet \subset Z^{0+}$ (Δ Hardy or not)	111
6 a. Proof of $Z^- \cap Z^+ \supset Z^{0+}$ (Δ Hardy or not)	113
6 b. Proof of $Z^{0+} = Z^\bullet$ (Δ Hardy)	114
6 c. A condition that $Z^- \cap Z^+ = Z^\bullet$ (Δ Hardy)	115
6 d. A condition that genus $Z^\bullet = 0$ (Δ Hardy)	118
6 e. Rational weights	120
7. A condition that $Z^{+/-} = Z^\bullet$ (Δ Hardy)	121
8. A condition that $Z^{0+} = Z$	123
9. Discussion of Z	124
10 a. Special case ($1/\Delta = 1 + c_1 a^2 + \text{etc.}$)	125
10 b. Special case ($\Delta = e^{-2 a ^{1/2}}$)	128
11. An example (Δ Hardy, $\dim Z_\bullet = \infty$, $Z^\bullet = Z^{0+} \neq Z_\bullet$)	130
12. Hardy weights with arithmetical gaps	133
13. Entire functions of positive type	135
14. Another condition for $Z^{+/-} = Z^{0+}$ (Δ Hardy)	142

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