

Subject Index

- Absolute 34, 35
Absoluteness 151
— Lemma, Shoenfield-Lévy 189
— —, Shoenfield's 195
— Principle, Lévy 76, 77, 243
Absolute version of a predicate 243
Abstract Kleene Theorem 231, 241
Acceptable structure 229
— —, almost 229
Aczel, P. 230, 380
— [1970] 230
 Aczel-Richter [1973] 187
 Richter-Aczel [1974] 205
Admissible fragment 97
— ordinal 45
— —, nonprojectible 174
— —, projectible 174
— —, recursively hyperinaccessible 185
— — — inaccessible 176
— — — Mahlo 187
— set above \mathfrak{M} 43
— —, original definition of 11
— — over \mathfrak{M} 43
— —, pure 44
— —, recursively listed 161, 164
— —, resolvable 163, 329
— —, $s\text{-}\Delta_1^1$ resolvable 332
— —, self-definable 257, 328
— — —, strongly 257
— — —, Σ_1 compact 257
— — —, Σ_1 complete 260
— — —, validity 260
Admit (κ, λ) , to 277
 \mathbb{A} -finite 153
a.i.d. 333
Almost all 353
Analysis 143
—, model of 143
 \mathbb{A} -r.e. 153
 \mathbb{A} -recursive 153
Assignment 82
Axioms A1-A7 92
- Back and forth property 292
Barwise, J. 116, 126, 380
— [1967] 4, 102, 291
— [1968] 333, 352
— [1969] 75, 102, 105, 109, 187
— [1969a] 4
— [1969b] 4, 333, 355
— [1971] 365, 366
— [1973] 102, 105, 303
— [1974] 9, 33, 365, 366
Barwise-Fisher [1970] 196
Barwise-Gandy-Moschovakis [1971] 116, 126, 220, 321
Barwise-Kunen [1971] 270, 276, 291
Beta 39
Beth's Theorem 104, 129
Borges, J. L. 364
Boundedness Theorem 234
Branch 311
Brouwer-König Infinity Lemma 314
- Canonical Scott Sentence 297, 301
— — Theory 300
— — structure 86
Cardinal, α - 187
— —, inaccessible 347
— —, Mahlo 355
— —, Σ_1 compact 357
— — —, strongly compact 364
— — —, weakly compact 356
Cartesian product 12
Chang, C. C. 127, 303, 380
— [1964] 127
— [1968] 262, 303
 Chang-Keisler [1973] 283, 350
 Chang-Makkai-Reyes Theorem 127, 131
 Chang-Moschovakis [1970] 241
Characteristic of s in \mathfrak{M} , α - 298
Church, A. 380
— [1938] 2
 Church-Kleene [1937] 2
Church's thesis 153

- Closed in κ 352
 Closure ordinal, Moschovakis 231
 — — of Σ_+ 210
 — Theorem 231
 Coding scheme 229
 Cohn, P. M. 303
 Coinductive 212
 —, Φ - 204
 Collapsing 39
 — function 29, 30
 — Lemma 32, 41, 53, 54
 Collection, Δ_0 10, 11
 —, full 39
 —, Σ 17
 Combination Lemma 217
 Compactness Theorem 101
 — —, Barwise 99, 102, 144
 — —, Kreisel 2
 — —, stable 187
 Compact, Σ_1 328
 Completeness Theorem, Barwise 99, 102
 — —, extended 100
 — — for Arbitrary Skolem Fragments, weak 266
 — — for countable fragments, weak 95
 — — for $L_{\omega_1\omega}$, karp 95
 — —, \mathfrak{M} - 89
 — —, ω 87, 92
 Complete Σ_1 set 328
 — strict- Π^1_1 set 328
 — theory 110
 Conjunction 81
 — rule 97
 Consistency machine 134
 — property 85, 109
 Constructible 58
 — from 58
 — sets 3, 29, 57
 — — with urelements 57
 Cotype, α -recursive 236
 Countable 14
 Cover of a model 367
 — — — model, admissible 367
 Craig, W. 1, 103
 — [1957] 105
 c.u.b. filter 353
 c.u.b. in κ 352
 Conjunction rule 93
 Cutland, N. 381
 Decidable structure 111
 Definability operator, general Δ 335
 Definable, invariantly 147
 —, semi-invariantly 147
 Definition, good Σ_1 61
 —, Σ_1 61
 Devlin, K. V. 381
 — [1973] 187
 Dickmann, M. A. 381
 Disjunction 81
 Divisible part of a group 117, 204
 Downward Löwenheim-Skolem-Tarski Theorem 269
 Ehrenfeucht, A. 381
 Ehrenfeucht-Kreisel [1966] 310
 Ehrenfeucht-Mostowski 278
 Elementary substructure, L_A - 268
 Enderton, H. 54, 381
 — [1972] 54
 End extension 34
 Engeler, E. 381
 Erdős-Rado Theorem 282, 285, 286
 Essentially uncountable 259
 Extension 34
 Extensionality 10
 Feferman, S. 381
 — [1968] 50
 — [1974] 37
 Feferman-Kreisel [1966] 35
 Field 14
 Finite 14
 — approximations 251
 —, notions of 174
 Fisher, E. 380
 Barwise-Fisher [1970] 196
 Fixed point 212
 — — of an inductive definition, largest 204
 — —, Φ - 203
 — —, Σ_+ 205
 — —, $\dot{\Sigma}(\uparrow \mathcal{K})$ 205
 Flum, J. 381
 Forcing 4, 146
 Formula, $\forall \exists$ - 191
 —, α -finite 235
 —, atomic 79
 —, finite 79
 —, game, closed 245
 —, —, open 242
 —, —, —, of an 251
 —, —, —, recursive 242
 —, infinitary 81
 —, orderly 64
 —, Π 15
 —, proper infinitary 81
 —, R-monotone 200
 —, R-positive 156
 —, Σ 15
 —, Σ_1 15
 —, strict- Π^1_1 316
 —, strict- Σ^1_1 316
 —, termed- 64

- Formulas, Δ_0 10
 —, first order, coextended 50
 —, —, extended 50
 Foundation 10
 Fragment 84
 Friedman, H. 107, 381
 — [1973] 109, 137, 365
 Friedman-Jensen [1968] 144
 Function 14
 — symbol, Σ 21
- Gaifman, H. 381
 Gale, D. 381
 Gale-Stewart 246
 Gale-Stewart Theorem 246
 Game, infinite two-person 244
 Gandy, R. O. 72, 116, 126, 211, 381
 — [1974] 211
 — [1975] 58, 72
 Barwise-Gandy-Moschovakis [1971] 220, 321
 Gandy-Kreisel-Tait Theorem 116
 Gandy's Theorem 208, 211, 377
 —, second half of 210
 Garland, S. J. 381
 Generalization 93
 Gödel, K. 1, 3, 8, 54, 57, 105, 382
 — [1939] 3, 62
 — [1940] 62
 Gödel numbers 154
 Gödel's operations 63
 Goofang 364
 Gordon, C. 382
 — [1970] 50, 51
 Grilliot, T. 382
 — [1972] 116
 Group, \aleph_1 -free abelian 303
 —, p - 297
 —, reduced abelian p - 297
 Grzegorczyk, A. 382
 Grzegorczyk, Mostowski and Ryll-Nardzewski [1959] 2
 Grzegorczyk, Mostowski and Ryll-Nardzewski [1961] 149
- Hanf, W. 291, 382
 — [1964] 262, 364
 Hanf-Scott [1961] 364
 Hanf number 276
 — — for Σ_1 theories 291
 — — for single sentences 290, 291
 — — of second order logic 351
 Harrison, J. 112, 127, 382
 Heatherton Rock Cakes 69
 Henkin, L. 87, 382
 Henkin [1949] 269
 — [1954] 92
 — [1957] 92
- Henkin argument 86
 Hereditarily finite 46
 Holmes, O. W. 5
 Hyperarithmetic 2, 60
 — sets 149
 Hyperelementary 212
 —*, *see* extended hyperelementary 214
 —, extended 214
 — Selection Theorem 240
 — substitution 221
- i.i.d. 333
 Implicit definition of an ordinal 314
 Indescribable, Π^1_1 358
 —, strict- Π^1_1 315, 358
 Indiscernibles 279
 —, k -variable 283
 — over U 279
 — — U , k -variable 283
 Induction over ϵ , proof by 24
 — — TC, proof by 26
 Inductive 212
 —*, *see* extended inductive 214
 — definition 197, 210
 — —, absoluteness of 207
 — —, α^{th} -iterate of an 198
 — —, closure ordinal of an 200
 — —, — ordinal of Σ_+ 218
 — —, extended 214
 — —, —, closure ordinal of an 215
 — —, —, first order positive 211
 — —, —, fixed point of an 197
 — —, —, point of an, smallest 197
 — —, — given by a formula 200
 — —, nonmonotonic 205
 — — on an essentially uncountable admissible set 262
 — —, — picture of an 199
 — — definitions, closure properties of 221
 — —, non-monotonic 4
 —, extended 214
 —, Φ - 203
 — relation, Σ_+ 205
 — —, $\Sigma(\mathcal{K})$ 205
 Infinitary proof 96
 Infinity 38
 Initial substructure 34
 Inner submodel 56
 Internal set 113, 115
 Interpolation Theorem 103, 129, 253, 261
 Interpretation 54, 56
 —, transitive \in - 56, 57, 59
 Invariant definability 333
 — relation 301
- Jech, T. 33, 382
 — [1973] 33

- Jensen, R. B. 72, 186, 187, 381, 382
 — [1972] 58, 62, 72
 Friedman-Jensen [1968] 144
 Jensen-Karp [1972] 196
- Karp, C. 382
 — [1965] 293
 — [1967] 262
 — [1968] 9, 352
 Jensen-Karp [1972] 196
- Karp's Theorem 294
- Keisler, H. J. 84, 383
 — [1965] 250
 — [1971] 84, 86, 87, 91, 92, 103, 270, 277, 283, 291
 — [1973] 365
 Chang-Keisler [1973] 283, 350
- Kino, A. 383
 Takeuti-Kino [1962] 196
- Kleene, S. C. 1, 3, 49, 201, 380, 383
 — [1938] 2
 — [1955] 2
 Church-Kleene [1937] 2
- Kleene's Theorem 2
- *T*-predicate 166
- Kleene structure, uniform 241
- König Infinity Lemma 311
 — Principle, first 321
 — —, second 322
 — —, third 323
 — Principles 311
- KP 3, 8, 11, 239
- KPU 3, 8, 239
- KPU⁺ 11
- KPU, axioms of 10, 11
 —, intuitive set theory in 11
 —, nonstandard model of 72
- Kreisel, G. 116, 255, 381, 383
 — [1959] 11
 — [1965] 11
 — [1968] 262
 — [1971] 9
 Ehrenfeucht-Kreisel [1966] 310
 Feferman-Kreisel [1966] 35
 Kreisel-Sacks [1965] 2, 168
- Kreisel Basis Theorem 315
 — Compactness Theorem 2
- Kripke, S. 3, 8, 37, 54, 126, 173, 177, 187, 383
 — [1963] 196
 — [1964] 3, 11
- Krivine, J. L. 383
 Krivine-McAloon [1973] 365
- Kueker, D. 33, 303, 383
 — [1968] 127, 303
 — [1972] 33
- Kunen, K. 380, 383
 — [1968] 262, 333, 364
- Barwise-Kunen [1971] 276, 291
 Kunen's example 121, 228, 229
- Language 79
- Lévy, A. 383
 — [1965] 10, 11, 53, 54, 72, 77, 196
- Löwenheim-Skolem Theorem, upward 276, 277
- Logic 5
 —, axioms of \mathfrak{M} - 88
 —, \mathfrak{M} - 88, 241
 —, ω - 88
- Lopez-Escobar, E. 383
 — [1965] 105
 — [1966] 109, 276
- Lyndon Interpolation Theorem 203
- Machover, M. 384
- \mathfrak{M} -admissible 45
- Mahlo cardinal 360
- Makkai, M. 127, 129, 143, 241, 384
 — [1964] 127
 — [1973] 129, 254
 — [1975] 310
- Malitz, J. 384
 — [1971] 262
- McAloon, K. 383
 Krivine-McAloon [1973] 365
- Metarecursion theory 2, 168
- Metatheory 76
- Model, see structure 138
 — Existence Theorem 84, 86, 95, 109, 269
 — — —, extended 87, 90, 93
 — — —, weak 266
- Module, Noetherian 325
- Modus Ponens 93
- Monotonic operator 197
- Montague, R. 49, 384
 — [1968] 49
- de Morgan, A. 158
- Morley, M. 384
 — [1965] 109, 291
 — [1967] 291
- Morley, V. 384
- Moschovakis, Y. N. 49, 116, 126, 173, 212, 221, 230, 242, 253, 380, 384
 — [1969a] 49
 — [1971] 242, 253
 — [1974] 173, 187, 203, 217, 221, 224, 229, 230, 232, 239, 240, 241, 242, 253
 — [1975] 205
 Barwise-Gandy-Moschovakis [1971] 220, 321
 Chang-Moschovakis [1970] 241
- Mostowski, A. 30, 381, 382, 384
 — [1949] 33, 41
 — [1961] 41
- Ehrenfeucht-Mostowski 278

- Grzegorczyk, Mostowski and Ryll-Nardzewski [1959] 2
 Grzegorczyk, Mostowski and Ryll-Nardzewski [1961] 149
- Nadel, M. 310, 384
 — [1971] 303, 310
 — [1974] 303, 310
 Nadel's Basis Theorem 306
 Natural number 13
 Nerode, A. 384
 Nerode's Theorem 334
 Norm 232
 —, inductive 232
 Normal Form Lemma 318
 — function 354
 Notation system 2, 168, 368
 — —, domain of a 168
 — — for IHF_{gr} 223, 227
 — —, univalent 172
 Nyberg, A. 230, 241, 334, 351
- Omitting Types Theorem 91
 Operation, Σ 23
 — symbol, substitutable 70
 Operator, general weak metarecursive 337
 Ordered n -tuples 13
 — pair 12
 Ordinal 13
 — addition 29
 —, admissible 60
 —, least nonrecursive 60
 — multiplication 29
 —, Π implicit 323, 339
 —, s - Σ_1^1 implicit 323, 341
 Orey, S. 87, 384
 — [1956] 92
- Pair 10, 11
 Pairing function 220
 Parametrization 154
 — of extended inductive relations 214
 — — first oder definable relations 171
 — — inductive relations 213, 235
 — — projections 171
 — — the class of Δ -r.e. relations 154
 Partial isomorphism 292
 Partially isomorphic structures 292
 Peano arithmetic 117, 126, 130, 137, 143, 144, 146, 158, 239
 Perfect set argument 110, 133, 137
 Persistent 34, 35
 Pinning down ordinals 105, 270
 Π_1^1 reflection 187
 Platek, R. 3, 8, 11, 54, 126, 173, 177, 187, 384
 — [1965] 3, 196
 — [1966] 11
 Power set axiom 40
- Predicate, absolute 33
 —, co-extended Σ_1^1 117
 —, Δ 21
 —, extended Π_1^1 117
 — of functions, r.e. 312
 — — integers, strict- Π_1^1 313
 —, persistent 33
 Predicates, Δ_0 14
 Prerequisites 1
 Prewellordering 164
 — Theorem 232
 Principle of parsimony 8, 13
 Projectible 168
 Projectum 174
 —, admissibility of 184
 Proof, L_{Δ} 97
 Pure part 44
 — set 44
 PZF 37
- Quantifier rank of a formula 296
- Rank function 29
 — —, \prec 161
 Recipe 69
 Recursion along well-founded Relations 158
 —, definition by Σ 26
 —, Δ predicates defined by 28
 — Theorem, second 156, 157, 159
 — —, ordinary 49
 Recursive ordinal 2
 Recursively saturated 74
 — — structure 138
 — Σ_1^1 saturated 348
 Reducibility, Δ definable 335
 — — —, truth table 335
 —, truth table 334
 —, Turing 334
 —, weak metarecursive 337
 Reduction Theorem for Δ -r.e. sets 165
 — — — inductive sets 240
 — — — Π_1^1 sets 167, 168
 Reflection Lemma, Π_2 185
 —, Π_1^1 358
 —, Σ 11, 16, 17
 —, s - Π_1^1 210
 —, strict- Π_1^1 322, 328
 Relation 14
 — symbol, Δ 19
 Relativization 15
 Replacement, Σ 17
 —, strong Σ 18
 Representability 149
 Representable, strongly 146, 147, 148
 —, weakly 146, 147, 148
 Resolution 163
 — of Π_1^1 sets 167, 168

- Ressayre, J.-P. 143
 Retraction, \in 370
 Reyes, G. E. 384
 — [1968] 127
 Richter, W. 384
 Aczel-Richter [1973] 187
 Richter-Aczel [1974] 205
 Rigid structure 302
 Rogers Jr., H. 385
 — [1967] 336
 Rule, \mathfrak{M} - 89
 —, ω - 88
 Rules R1–R3 93
 Ryll-Nardzewski, C. 382
 Grzegorczyk, Mostowski and Ryll-Nardzewski [1959] 2
 Grzegorczyk, Mostowski and Ryll-Nardzewski [1961] 149
- Sacks, G. E. 144, 151, 383
 Kreisel-Sacks [1965] 2, 168
 Sacks school 338
 Satisfaction 82
 Schlipf, J. 139, 143, 241
 Scott, D. 303, 382, 385
 — [1964] 303
 — [1965] 303
 Hanf-Scott [1961] 364
 Scott rank of a structure 300
 Scott's Theorem 301
 Search computable 49, 50
 — —, semi- 49, 50, 51
 Second order arithmetic 143
 Section 203
 Semantics 78
 — of $L_{\infty\omega}$ 82
 Separation, Δ 17
 —, Δ_0 10, 11
 —, full 38
 —, Σ_1 38, 39, 41
 — Theorem for co- \mathbb{A} -r.e. sets 165
 — — — coinductive sets 240
 — — — Π_1^1 sets 167, 168
 Shoenfield, J. R. 1, 54, 196, 385
 — [1961] 196
 — [1967] 7, 48, 54, 56, 116, 314, 315
 s.i.i.d. 333
 Simpson, S. G. 177, 339, 385
 — [1974] 177
 Skolem fragment 263
 — — with constants 263
 — function symbol 263
 — $\forall\exists$ normal form 192
 — structure 263
 — theory 263
 Smullyan, R. 385
- Special form 268
 — set of sentences 132
 Spector, C. 385
 — [1959] 201
 — [1961] 230
 Spector class 4
 Splitting 337
 Stable 3
 — ordinal 178
 — —, β - 179
 — —, the first 189
 Stavi, J. 310
 Stewart, F. M. 381
 Gale-Stewart 246
 Strategy 244
 Stretching Theorem 279
 Structure 81
 — for L^* 10
 —, \mathfrak{M} - 88
 —, resplendent 351
 Subformula 81
 Substitutable function, *see* substitutable operation symbol 70
 — operation, *see* substitutable operation symbol 70
 Subtree 311
 Superstable 353
 Supertransitive 346
 Supervalidity property 265
 Support function 24, 29
 Suzuki, Y. 385
 Suzuki-Wilmers [1973] 365
 Svenonius, L. 248, 253, 385
 — [1965] 242
 Svenonius' Theorem 248, 352
 s.v.p., *see* supervalidity property 265
 Syntax 78
 —, axioms on 79
 — of $L_{\infty\omega}$ 81
- Table 1 14
 — 2 22
 — 3 23
 — 4 29
 — 5 254
 Tague, T. 385
 — [1964] 3
 Tait, W. 116, 381
 Takeuti, G. 3, 54, 383, 385
 — [1960] 3, 187
 — [1961] 3
 Takeuti-Kino [1962] 196
 Tarski 262
 — criterion for \prec_1 180
 Term 79
 —, basic 84
 t-formula, *see* termed-formula 64
 Theorem of L_A 94

- Torsion part of a group 117
- Transitive closure 24
- Translation Lemma 376
- Tree 343
 - , \mathbb{A} - 344
 - argument, *see* perfect set argument 110
 - , branch thru a 344
 - , complete binary 110
 - , full binary 311
 - , κ - 361
 - , path thru a 344
 - property 361
- Truncation Lemma 73, 75
- Two cardinal model of type (κ, λ) 277
 - — models 288
 - — Theorem 277
 - — —, Morley's 277
- Type, α -recursive 235
- UCLA Logic year 211
- Unbounded in κ 352
- Uniformization Theorem for \mathbb{A} -r.e. sets 165
 - — — Π_1^1 sets 167
- Uniformly equivalent 330
- Union 10, 11
- of chain lemma 267, 268
- Urelement 7, 10, 69
- Validity property 92, 93
 - —, smallest 93
- Variables, convention on 10, 13, 16, 157
- Vaught, R. 385
 - [1973] 253
- Ville, F. 75, 385
 - [1974] 116
- Weakly compact cardinal 357
- Weak second-order logic 51
- Well founded 39
 - — part 73
- Well-ordering 41
 - , definable 105
 - of L 162
- Wilmers, G. 385
 - [1973] 365
 - Suzuki-Wilmers [1973] 365
- Zermelo 9
- ZF 7, 8, 239